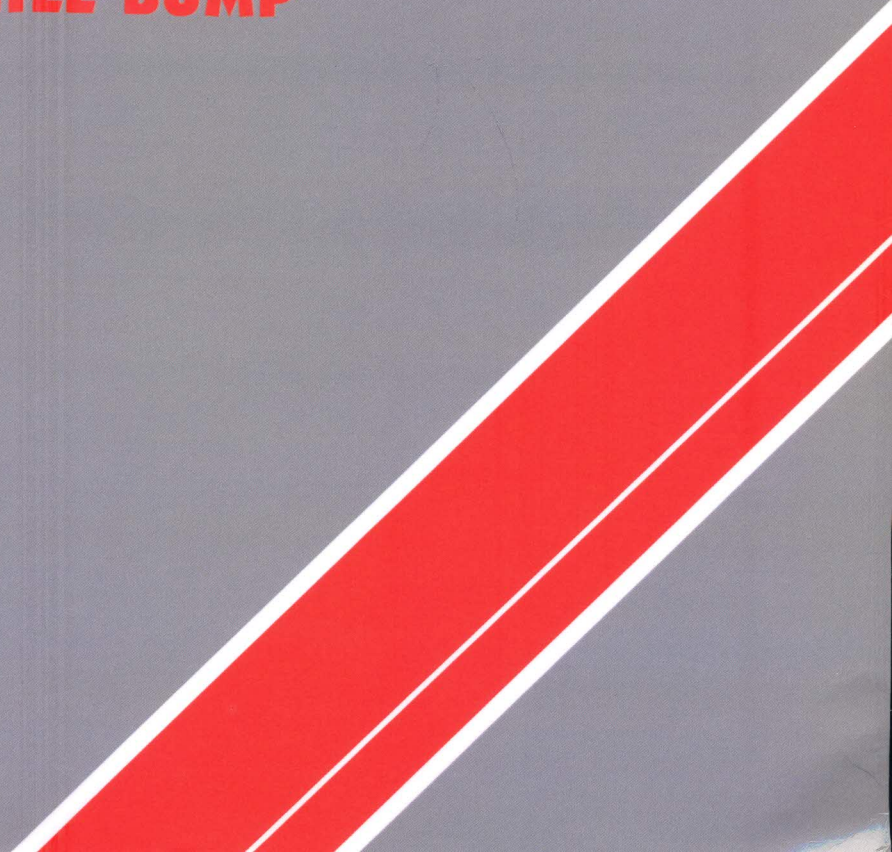


Cambridge Studies in Advanced Mathematics 55

Automorphic Forms and Representations

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